

COURSE OBJECTIVES LIST: ALGEBRA II

Algebra II Honors is offered.

PREREQUISITES: All skills from Algebra I and Geometry are assumed. A prerequisites test may be given during the first week of class to assess knowledge of these prerequisite skills and to locate deficiencies.

COURSE DESCRIPTION:

Algebra II develops the tools introduced in the previous algebra course, while introducing many more concepts and exploring real-life applications. Topics include recursion, probability and statistics, systems, matrices, polynomials, rational functions, exponential and logarithmic functions, graphical transformations, periodic functions, and parametric equations. One central issue is the relationship between the algebraic and the graphical representations of information; the graphing calculator is used extensively in exploring this interplay. An honors section encourages more creative, critical and in-depth study of these topics.

The course objectives are elaborated as follows. The order in which the objectives are listed is not necessarily the order in which they will be taught.

- matrix notation: matrix (matrices); dimensions of a matrix; element; equality of matrices
- arithmetic with matrices: adding/subtracting; multiplying by a constant; matrix multiplication
- the set of complex numbers (\mathbb{C}): $a + bi$ form; plotting points in the complex plane; arithmetic with complex numbers (adding/subtracting, multiplying); complex conjugate
- completing the square technique (apply to graphing circles)
- logarithms: the number $\log_b x$ should be understood from two points of view. Firstly, it is the *exponent* that b must be raised to, in order to get x . Secondly, the function $\log_b x$ “undoes” the function b^x .
- logarithm terminology: common logs, natural logs
- change of base formula for logarithms
- properties of logarithms: for positive numbers x and y , $\ln xy = \ln x + \ln y$, $\ln \frac{x}{y} = \ln x - \ln y$, $\ln x^y = y \ln x$
- basic concept of probability: a probability is a number between 0 and 1 that represents the likelihood of occurrence of something; calculating simple probabilities
- combinations versus permutations; distinguishing between the two; formulas for each
- sequences: recursive versus nonrecursive; arithmetic and geometric; function and subscript notation; loans and investment applications; compound interest formula; graphing sequences

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- statistics: mean, median, mode; measures of spread (variance and standard deviation)
- parametric equations: can be used to generate a graph swept out in time; converting from parametric to non-parametric form; applications
- functions: review concept; review function notation
- Graph of a function: a picture of all its (input,output) pairs. By convention, the inputs are on the horizontal axis, and the outputs on the vertical axis. The label “ $y = f(x)$ ” states that each y -value is the output from the function f when the input is x .
- recognize functions from a formula, verbal descriptions, tables, graphs
- Understand the phrase: “ y is a function of x ”. Recognize when y is a function of x ; when x is a function of y (from words, tables, graphs)
- composition of functions: evaluation (given $f(x)$ and $g(x)$, find $f(g(x))$)
- Understand the equivalence of two common requests:
Graph the equation $y = x^2$. That is, show all the points that make the equation true: $(x, y) = (x, x^2)$.
and
Graph the function $f(x) = x^2$. That is, show all the input/output pairs: $(x, f(x)) = (x, x^2)$.
- familiarity with these “basic models”: $y = x$, $y = x^2$, $y = x^3$, $y = |x|$, $y = \sqrt{x}$, $y = \frac{1}{x}$, and $y = k$. Given the equation, know the shape of the graph. Given the graph, identify the (probable) equation.
- Explain the graphical interpretation of the solution set of sentences of the form $f(x) = 0$, $f(x) > 0$, etc. For example, the solution set of $f(x) = 0$ is the set of x -intercept(s) for the graph of f .
- Explain the graphical interpretation of the solution set of sentences of the forms $f(x) = g(x)$, $f(x) > g(x)$, etc. For example, the solution set of $f(x) = g(x)$ is the set of x -value(s) of the intersection point(s) of the graphs of f and g .
- horizontal and vertical translations: going from $y = f(x)$ to $y = f(x \pm c)$ and $y = f(x) \pm c$
- vertical scaling: going from $y = f(x)$ to $y = kf(x)$
- reflection about the x -axis: going from $y = f(x)$ to $y = -f(x)$
- Apply the techniques discussed above to graph a wide variety of functions/equations without the use of a graphing calculator. (However, a graphing calculator may be used to verify results.) For example, be able to graph $y = -\sqrt{x-7} + 3$ without a calculator.
- solve any quadratic equation $ax^2 + bx + c = 0$; the quadratic formula
- solve exponential equations like $2^x = 5$
- solve logarithmic equations like $\log_2 x = 5$
- review lines and slope

- linear systems of equations in 2 variables: solution of a system by both the substitution and elimination techniques; graphical interpretations
- writing a linear system in matrix form
- solving simple nonlinear systems of equations/inequalities in 2 variables, like $y = x^2$, $y = x + 1$
- quadratic functions: $y = ax^2 + bx + c$ and $y = a(x - h)^2 + k$ forms; graph as parabolas; vertex
- polynomials: definition; degree
- review properties of exponents
- exponential functions: allowable bases; growth versus decay
- logarithmic functions: allowable bases; shapes of graphs for different bases
- rational functions: horizontal and vertical asymptotes;
Use notation like: as $x \rightarrow -1^+$, $y \rightarrow -\infty$.
Distinguish between puncture points (holes) and vertical asymptotes.
- periodic functions: periodicity; brief exposure to the cosine and sine functions as x and y values of points on the unit circle. Show the relationship to the right triangle definitions that were studied in geometry.